

Distinguishing between R^2 and Higgs inflation

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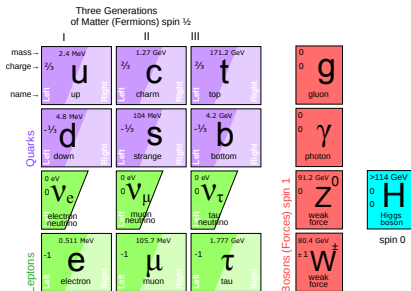
Outline

- 1 Why should one want to compare R^2 and Higgs inflation
 - SM is great but definitely not the end of the story
 - ν MSM for “late” cosmology
- 2 Inflation?
 - R^2 inflation
 - Higgs inflation
- 3 Distinguishing R^2 and Higgs inflation
 - CMB predictions
 - Gravity waves
 - Higgs boson mass
- 4 Conclusions

Standard Model – describes nearly everything that we know

Gauge theory $SU(3) \times SU(2) \times U(1)$
 Describes (together with
 Einstein gravity)

- all laboratory experiments
 – electromagnetism,
 nuclear processes, etc.
- all processes in the
 evolution of the Universe
 after the Big Bang
 Nucleosynthesis
 ($T < 1 \text{ MeV}$, $t > 1 \text{ sec}$)



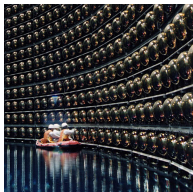
Standard Model has **experimental** problems

- Laboratory
 - Neutrino oscillations
- Cosmology
 - Baryon asymmetry of the Universe
 - Dark Matter
 - Inflation
 - Horizon problem (and flatness, entropy, ...)
 - Initial density perturbations
 - Dark Energy

Neutrino oscillations



SAGE neutrino observatory
 (solar oscillations evidence
 $\nu_e \rightarrow \nu_\mu$)

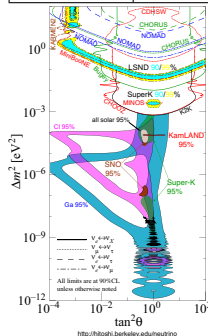


SuperKamiokande
 (atmospheric oscillations
 $\nu_\mu \rightarrow \nu_\tau$)

Reactor neutrinos, accelerator neutrinos

Oscillation parameters

Δm_{21}^2	$7.59 \pm 0.20 \times 10^{-5} \text{ eV}^2$
$\sin^2 2\theta_{12}$	0.87 ± 0.03
$ \Delta m_{32}^2 $	$2.43 \pm 0.13 \times 10^{-3} \text{ eV}^2$
$\sin^2 2\theta_{23}$	> 0.92
$\sin^2 2\theta_{13}$	< 0.15



Baryon asymmetry of the Universe

- Current universe contains baryons and no antibaryons
- Current baryon density

$$\eta_B \equiv \frac{n_B}{n_\gamma} \simeq 6.1 \times 10^{-10}$$

- Does not fit into the SM (too weak CP violation, too smooth phase transition)

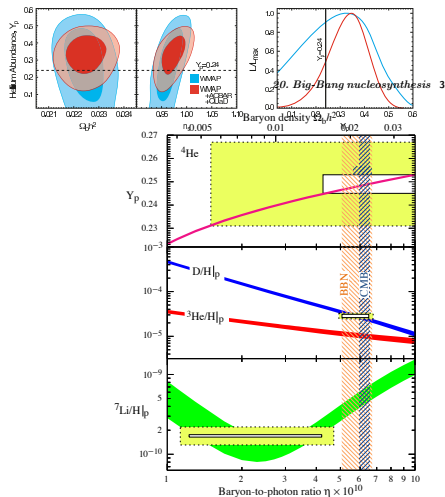
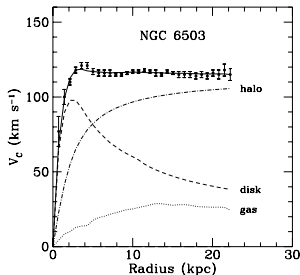


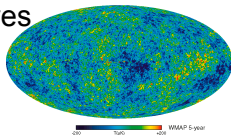
Figure 20.1: The abundances of ${}^4\text{He}$, D , ${}^3\text{He}$, and ${}^7\text{Li}$ as predicted by the standard model of Big-Bang nucleosynthesis [11] – the bands show the 95% CL range. Boxes

Dark Matter



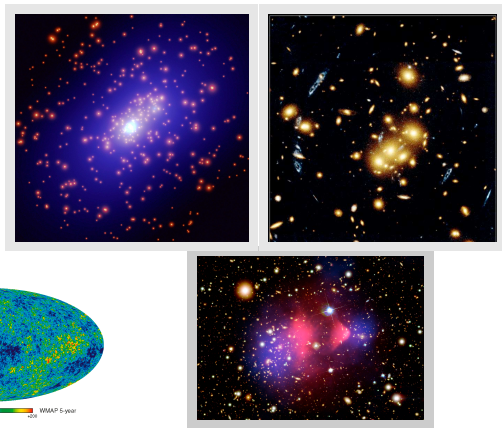
Rotation curves

$$\Omega_{DM} \simeq 0.21$$



CMB fluctuations

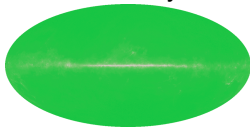
Gravitational lensing



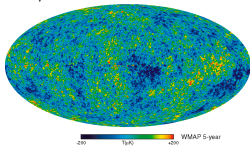
"Bullet" cluster

Inflation evidence – horizon problem

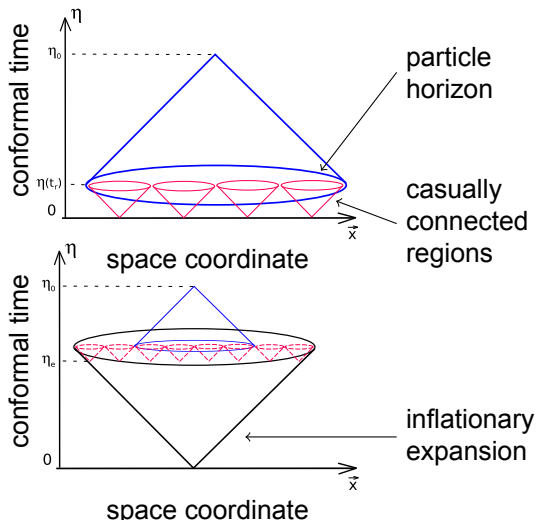
Microwave sky



Temperature
 fluctuations
 $\delta T/T \sim 10^{-5}$

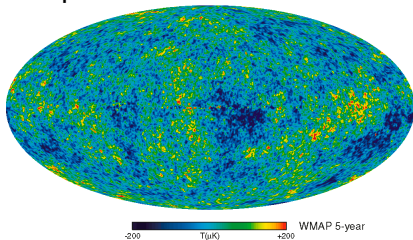


Universe is **uniform!**

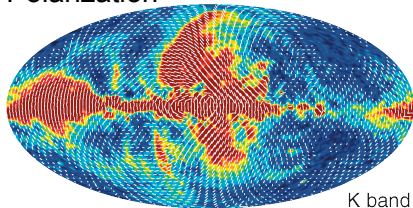


CMB gives measured predictions from inflation

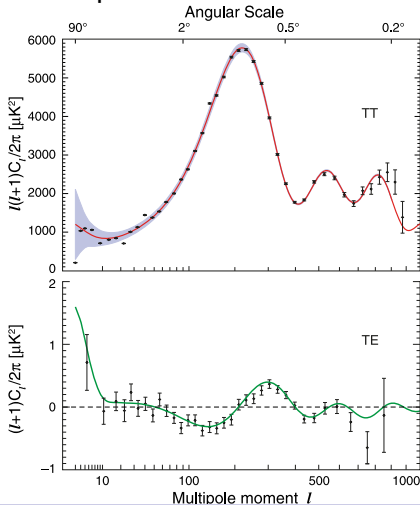
Temperature fluctuations



Polarization

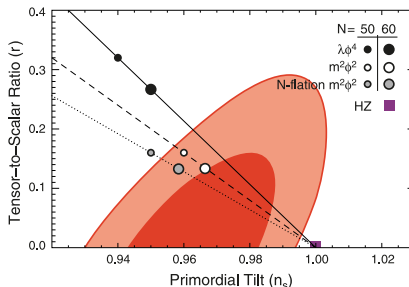


CMB spectrum



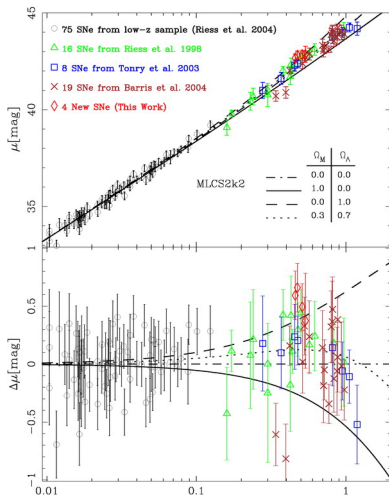
Inflationary parameters from CMB

- Spectrum of primordial scalar density perturbations is just a bit not flat $n_s - 1 \equiv \frac{d \log \mathcal{P}_{\mathcal{R}}}{d \log k}$
- Tensor perturbations are compatible with zero $r \equiv \frac{\mathcal{P}_{\text{grav}}}{\mathcal{P}_{\mathcal{R}}}$



(WMAP07 results)

Dark Energy



← Supernova type Ia redshifts

accelerated expansion of the
 Universe today

$$\Omega_\Lambda \simeq 0.74$$

Different from inflation

- Much lower scale
- No need to stop it

Can be explained “just” by a
cosmological constant

Let us expand the model in a minimal way

I will follow a “Minimal” approach

Explain the **experimental** facts with

- minimal number of new particles
 - no new physical scales
-
- Higgs boson inflation
 - R^2 inflation
 - ...
- } + ν MSM

Dark matter, BAU – just add sterile neutrinos (ν MSM)

gravity + inflation +

Three Generations of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III	
mass	2.4 MeV	1.27 GeV	171.2 GeV	
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
name	u up	c charm	t top	g gluon
	d down	s strange	b bottom	γ photon
Quarks				Z^0 weak force
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	H Higgs boson
	N_1 sterile neutrino	N_2 sterile neutrino	N_3 sterile neutrino	
Leptons				
	e electron	μ muon	τ tau	
				W^\pm weak force

Bosons (Forces) spin 1

spin 0

[Asaka, Blanchet, Shaposhnikov'05]

- DM sterile neutrinos are produced by oscillations from active neutrinos
- Two heavier sterile neutrinos provide for the baryon asymmetry (via low scale leptogenesis)

R^2 inflation

Modifying the gravity action gives inflation

The first working inflationary model

[Starobinsky'80]

The gravity action gets higher derivative terms

$$S_J = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R + \frac{\zeta^2}{4} R^2 \right\} + S_{SM}$$

Conformal transformation

conformal transformation (change of variables)

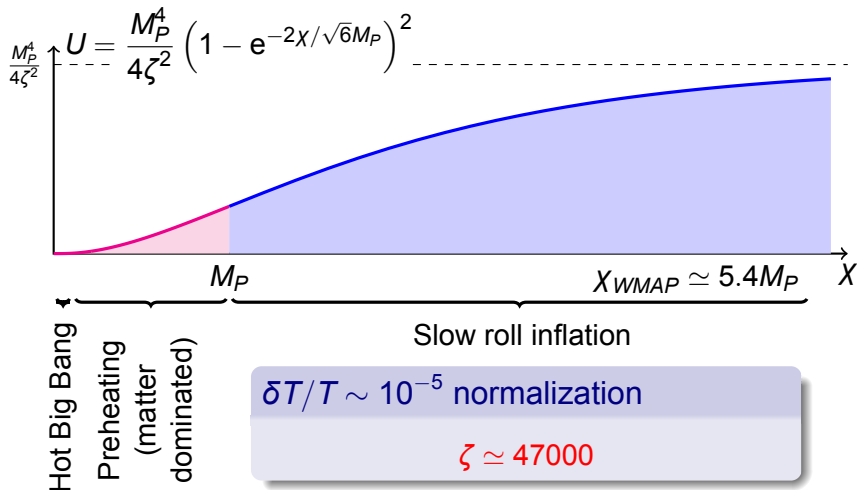
$$\hat{g}_{\mu\nu} = \Omega^2 g_{\mu\nu}, \quad \Omega^2 \equiv \exp\left(\frac{X(x)}{\sqrt{6}M_P}\right)$$

$\chi(x)$ — new field (d.o.f.) “scalaron”

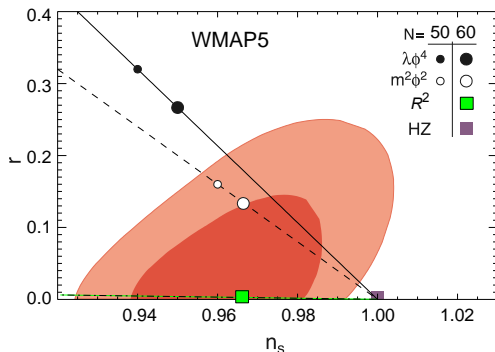
Resulting action (Einstein frame action)

$$S_E = \int d^4x \sqrt{-\hat{g}} \left\{ -\frac{M_P^2}{2} \hat{R} + \frac{\partial_\mu X \partial^\mu X}{2} - \frac{M_P^4}{4\zeta^2} \left(1 - e^{-\frac{2X}{\sqrt{6}M_P}} \right)^2 \right\}$$

Inflationary potential



CMB parameters are predicted



spectral index $n \simeq 1 - \frac{8(4N+9)}{(4N+3)^2} \simeq 0.97$

tensor/scalar ratio $r \simeq \frac{192}{(4N+3)^2} \simeq 0.0033$

Reheating is due to the Planck suppressed terms

Jordan frame action – matter

$$S_J^{\text{scalar}} = \int d^4x \left\{ \frac{1}{2} \partial \varphi \partial \varphi - \frac{m_\varphi^2}{2} \varphi^2 \right\}$$

$$S_J^{\text{fermion}} = \int d^4x \{ i \bar{\psi} \not{D} \psi - m_\psi \bar{\psi} \psi \}$$

$$\hat{\varphi} = \Omega^{-1} \varphi$$

$$\hat{\psi} = \Omega^{-3/2} \psi$$

$$\Omega^2 \equiv \exp \left(\frac{\chi(x)}{\sqrt{6} M_P} \right)$$

Einstein frame action – χ interactions are M_P suppressed

$$S_E^{\text{scalar}} = \int d^4x \left\{ \frac{1}{2} \Omega^{-2} \partial(\Omega \hat{\varphi}) \partial(\Omega \hat{\varphi}) - \frac{m_\varphi^2}{2} \Omega^{-2} \hat{\varphi}^2 \right\}$$

$$S_E^{\text{fermion}} = \int d^4x \{ i \bar{\hat{\psi}} \not{D} \hat{\psi} - m_\psi \Omega^{-1} \bar{\hat{\psi}} \hat{\psi} \}$$

Reheating happens at relatively low temperature

- Scalaron decay ($\mu = M_P/(\sqrt{3}\zeta)$ is the scalaron mass)

$$\Gamma_{\chi \rightarrow \varphi\varphi} = \frac{\mu^3}{192\pi M_P^2} \quad \Gamma_{\chi \rightarrow \bar{\psi}\psi} = \frac{\mu m_\psi^2}{48\pi M_P^2}$$

- Main decay contribution is from the non-conformal kinetic term of the scalar
- No resonant enhancement (near immediate rescattering of the decay products)

Reheating temperature from the scalaron decay

$$T_r \approx 3.5 \times 10^{-2} g_*^{-1/4} \sqrt{\frac{N_s}{\zeta}} \approx 3.1 \times 10^9 \text{ GeV}$$

[Gorbunov, Panin'11]

Higgs inflation

Non-minimal coupling to gravity solves the problem

Quite an old idea

Add $h^2 R$ term (required by renormalization) to of the usual $M_P R$ term in the gravitational action

- A.Zee'78, L.Smolín'79, B.Spokoiny'84
- D.Salopek J.Bond J.Bardeen'89

Scalar part of the (Jordan frame) action

$$S_J = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \xi \frac{h^2}{2} R + g_{\mu\nu} \frac{\partial^\mu h \partial^\nu h}{2} - \frac{\lambda}{4} (h^2 - v^2)^2 \right\}$$

- h is the Higgs field; $M_P \equiv \frac{1}{\sqrt{8\pi G_N}} = 2.4 \times 10^{18} \text{ GeV}$
- SM higgs vev $v \ll M_P / \sqrt{\xi}$

Conformal transformation – way to calculate

It is possible to get rid of the non-minimal coupling by the **conformal transformation** (change of variables)

$$\hat{g}_{\mu\nu} = \Omega^2 g_{\mu\nu}, \quad \Omega^2 \equiv 1 + \frac{\xi h^2}{M_P^2}$$

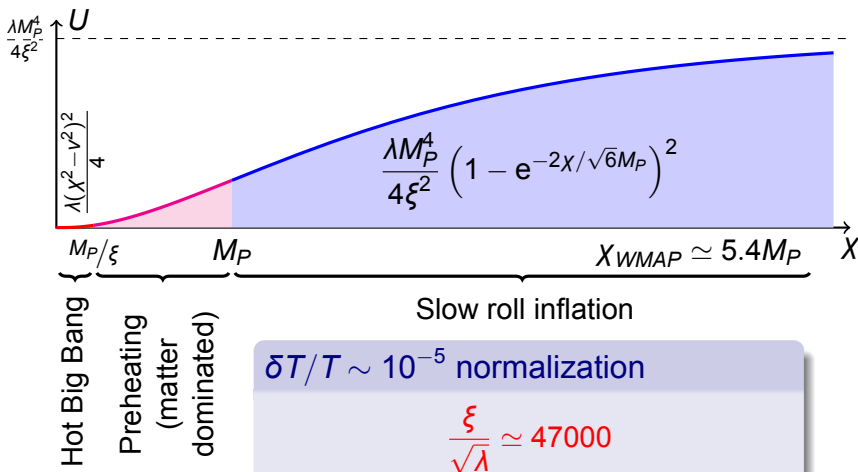
Redefinition of the Higgs field to get canonical kinetic term

$$\frac{d\chi}{dh} = \sqrt{\frac{\Omega^2 + 6\xi^2 h^2 / M_P^2}{\Omega^4}} \implies \begin{cases} h \simeq \chi & \text{for } h < M_P/\xi \\ \Omega^2 \simeq \exp\left(\frac{2\chi}{\sqrt{6}M_P}\right) & \text{for } h > M_P/\xi \end{cases}$$

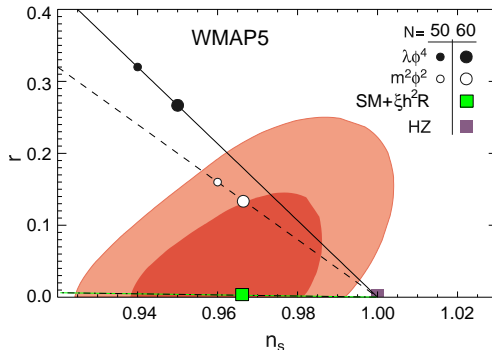
Resulting action (Einstein frame action)

$$S_E = \int d^4x \sqrt{-\hat{g}} \left\{ -\frac{M_P^2}{2} \hat{R} + \frac{\partial_\mu \chi \partial^\mu \chi}{2} - \frac{\lambda h(\chi)^4}{4 \Omega(\chi)^4} \right\}$$

Potential – different stages of the Universe



CMB parameters are predicted

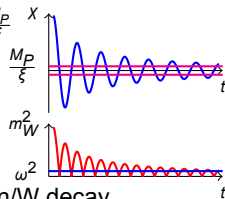


spectral index $n \simeq 1 - \frac{8(4N+9)}{(4N+3)^2} \simeq 0.97$

tensor/scalar ratio $r \simeq \frac{192}{(4N+3)^2} \simeq 0.0033$

Preheating

- Background evolution after inflation $\chi < M_P$ ($h < M_P/\sqrt{\xi}$)
 - Quadratic potential $U \simeq \frac{\mu^2}{2} \chi^2$ with $\mu = \sqrt{\frac{\lambda}{3}} \frac{M_P}{\xi}$
 - Matter dominated stage $a \propto t^{2/3}$
- Stochastic resonance
 - Particle masses $m_W^2(\chi) \sim g^2 \frac{M_P |\chi|}{\xi}$
 - W bosons are created (non-relativistic)
 - $\sqrt{\langle \chi^2 \rangle} \gtrsim 23 \left(\frac{\lambda}{0.25} \right)^{1/2} \frac{M_P}{\xi}$: non-resonant creation/W decay
 - $\sqrt{\langle \chi^2 \rangle} \lesssim 23 \left(\frac{\lambda}{0.25} \right)^{1/2} \frac{M_P}{\xi}$: resonant creation/W annihilation
 - Higgs creation – relativistic, less efficient



Reheating at

$$T_r \gtrsim 3.4 \times 10^{13} \text{ GeV}$$

[FB, Gorbunov, Shaposhnikov'08]. [Garcia-Bellido, Figueroa, Rubio'09]

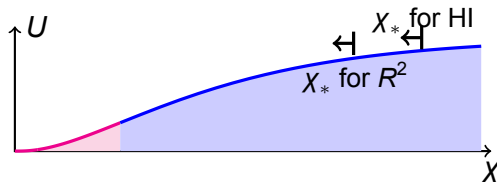
Different T_r means different field at horizon exit

- Hubble at the Horizon exit $H_* = \frac{k}{a_0} \frac{a_0}{a_r} \frac{a_r}{a_e} e^{N_*}$

$$\frac{a_r}{a_0} = \left(\frac{g_0}{g_r} \right)^{1/3} \frac{T_0}{T_r}, \quad \frac{a_r}{a_e} = \left(\frac{V_e}{g_r \frac{\pi^2}{30} T_r^4} \right)^{1/3}$$

- E-folding number of the horizon exit

$$N_* \simeq 57 - \frac{1}{3} \log \frac{10^{13} \text{ GeV}}{T_r} \Rightarrow N_{HI} = 57.7, \quad N_{R^2} = 54.4$$



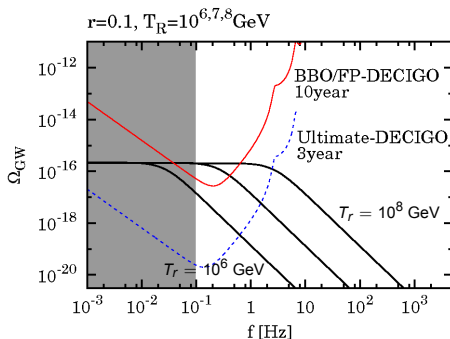
Different predictions for CMB observables

Higgs inflation: $n_s = 0.967$, $r = 0.0032$

R^2 inflation: $n_s = 0.965$, $r = 0.0036$

- Planck $\Delta n_s \sim 0.0045$ — not there, but not too far away
- CMBPol $\Delta n_s \sim 0.0016$, $\delta r \sim 10^{-3}$

Features in tensor perturbations for gravity wave detectors

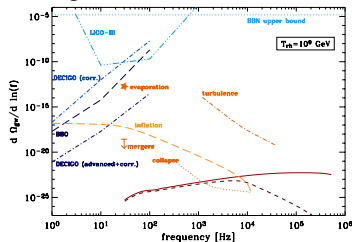


[Kuroyanagi et.al.'11]

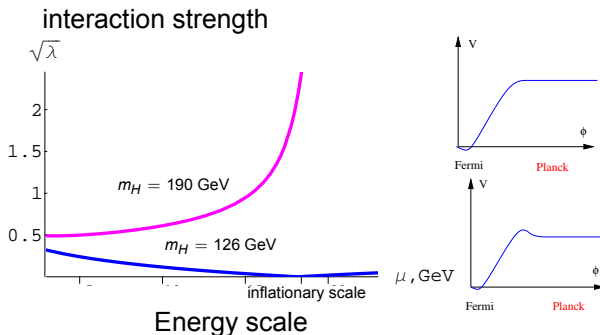
Gravity waves at matter dominated stage

- Primordial density of scalar perturbations $\delta\rho/\rho \sim 10^{-5}$
- Grow \propto scalefactor at matter domination
- Can reach $\delta\rho/\rho \sim 1$ for long matter domination and small scales, generating scalaron (inflaton) “clumps”
- Gravity waves can be generated
 - collapse of scalaron perturbations
 - merging of clumps
 - evaporation of clumps at reheating

For R^2 inflation can be in
 DECIGO reach
[\[Jedamzik et.al.'10\]](#)



Higgs mass bound in the Higgs inflation



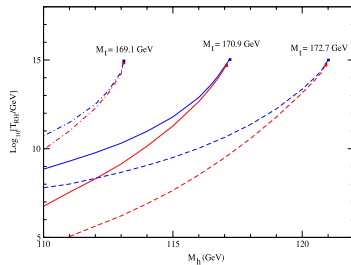
Higgs mass bound

$$m_H > 128.9 \text{ GeV} + \frac{m_t - 172.9}{1.1} \times 2.2 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.56$$

[FB, Magnin, Shapshnikov'08, FB, Shaposhnikov'09]

No (weak) Higgs mass bounds in the R^2 inflation

The electroweak vacuum may decay at high temperature



Higgs mass bounds in R^2

$$m_H > 116.5 \text{ GeV} + \frac{m_t - 172.9}{1.1} \times 2.2 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.56$$

[Espinosa, Giudice, Riotto'08]

- If SM (ν MSSM) is valid up to the inflationary scale —
 - still can explain all observable experimental facts
 - while nothing (except Higgs boson) is seen on LHC
- Inflation can be provided in several ways, with seemingly equivalent potentials
 - Higgs inflation (non-minimally coupled to gravity)
 - R^2 inflation
- Models can be distinguished, due to different evolution **after** inflation
 - slightly different CMB predictions
 - gravity wave signatures
 - Higgs inflation may be excluded by discovery of a light Higgs boson

Radiative corrections modify the inflationary potential

If we assume

- the full UV theory respects the scale invariance at high fields (or shift invariance in the Einstein frame)
- the quadratic divergences are subtracted to zero (e.g. work in dimensional regularisation)

then we can compute the radiative corrections to the inflationary potential *and* relate them to the parameters of the low energy physics (Higgs boson mass).

[\[FB, Sibiryakov, Shaposhnikov'10\]](#)

Prescription to calculate potential with radiative corrections

- 1 Run all constants with SM two-loop RG equations from the EW scale up to $M_P/\sqrt{\xi}$
- 2 Run all constants $\lambda_i(\mu)$ with chiral EW theory RG equations up to scale μ equal to a typical particle mass for the given field background χ

$$\mu^2 = \kappa^2 m_t^2(\chi) = \kappa^2 \frac{y_t(\mu)^2}{2} \frac{M_P^2}{\xi(\mu)} \left(1 - e^{-\frac{2\chi}{\sqrt{6}M_P}} \right).$$

- 3 Calculate the effective potential
 $U(\chi) = U_{\text{tree}}(\lambda_i(\mu), \chi) + U_{1\text{-loop}}(\lambda_i(\mu), \chi) + U_{2\text{-loop}}(\lambda_i(\mu), \chi)$
- 4 Calculate the inflationary properties for the resulting potential

[FB, Magnin, Shapshnikov'08, FB, Shaposhnikov'09]

Light inflaton model adds one scalar particle to the SM

$$\mathcal{L} = \underbrace{\mathcal{L}_{\text{SM}}}_{\text{Standard Model}} + \underbrace{\alpha H^\dagger H X^2}_{\text{Interaction}} + \underbrace{\frac{\beta}{4} X^4}_{\text{Inflationary sector}}$$

(where $\beta \simeq \beta_0 = 1.5 \times 10^{-13}$ – inflationary requirement)

$$m_X = m_h \sqrt{\frac{\beta}{2\alpha}} \quad - \text{the inflaton mass is defined by } \alpha$$

The Higgs-inflaton scalar potential is

$$V(H, X) = \lambda \left(H^\dagger H - \frac{\alpha}{\lambda} X^2 \right)^2 + \frac{\beta}{4} X^4 - \frac{1}{2} \mu^2 X^2 + V_0$$

[Anisimov, Bartocci, FB'08, FB, Gorbunov'09]

-  A.Starobinsky, Phys.Lett.B91 (1980) 99
-  FB, M. Shaposhnikov, Phys. Lett. B **659**, 703 (2008)
-  D.Gorbunov, A.Panin, Phys.Lett. B700 (2011) 157
-  FB, D. Gorbunov, M. Shaposhnikov, JCAP **06**, 029 (2009)
-  FB, A. Magnin, M. Shaposhnikov, Phys. Lett. B **675**, 88 (2009)
-  FB, A. Magnin, M. Shaposhnikov, S. Sibiryakov, JHEP **1101**, 016 (2011).
-  arxiv:0812.4624
-  FB, M. Shaposhnikov, JHEP **0907** (2009) 089
-  A. Anisimov, Y. Bartocci, F. L. Bezrukov, Phys. Lett. B **671**, 211 (2009)
-  FB, D. Gorbunov, JHEP **05** (2010) 010
-  T. Asaka, M. Shaposhnikov, Phys. Lett. B **620** (2005) 17
-  T. Asaka, S. Blanchet, M. Shaposhnikov, Phys. Lett. B **631** (2005) 151